

XII. Oven temperature at Chewy Pizza restaurants was in control when these samples were taken. Construct an \bar{x} chart and an R chart for this data using a 99.74% confidence interval.

Sample #	1	2	3	4	5	6	Totals
Oven Readings n = 3 N = 6 samples	405	402	398	410	391	411	
	404	404	390	402	409	409	
	397	412	388	412	400	407	
Sample Mean	402	406	392	408	400	409	2,417
Sample Range	8	10	10	10	18	4	60

ASTM Control Factors for 99.74%			
Sample Size (n)	A ₂	D ₃	D ₄
2	1.880	0	3.267
3	1.023	0	2.575
4	0.729	0	2.282
5	0.577	0	2.115

$$\bar{\bar{x}} = \frac{\sum \bar{x}}{N} = \frac{2,417}{6} = 402.83 \approx 402.8$$

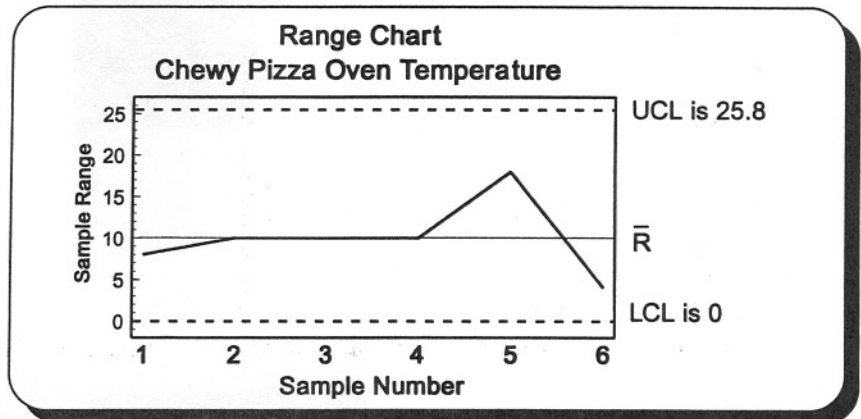
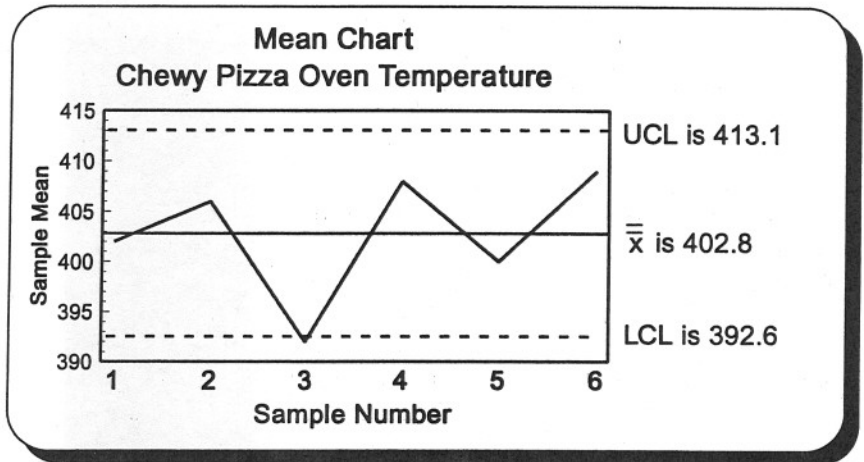
$$\bar{R} = \frac{\sum R}{N} = \frac{60}{6} = 10.0$$

$$\begin{aligned} \text{UCL} &= \bar{\bar{x}} + A_2 \bar{R} \\ &= 402.83 + 1.023(10) \\ &= 402.83 + 10.23 \\ &= 413.06 \\ &\approx 413.1 \end{aligned}$$

$$\begin{aligned} \text{LCL} &= \bar{\bar{x}} - A_2 \bar{R} \\ &= 402.83 - 1.023(10) \\ &= 402.83 - 10.23 \\ &= 392.6 \end{aligned}$$

$$\begin{aligned} \text{UCL} &= D_4 \bar{R} \\ &= 2.575(10) \\ &= 25.75 \\ &\approx 25.8 \end{aligned}$$

$$\begin{aligned} \text{LCL} &= D_3 \bar{R} \\ &= 0(10) \\ &= 0 \end{aligned}$$



XIII. Potential customers were asked to rate brand A and brand B. Little is known about the population distributions. Test at the .10 level of significance whether these brands were viewed equally by these potential customers. A paired difference sign test may be conducted even though this is not a test for statistical dependency.

Brand Preference Test			
Potential Customer	Brand A	Brand B	Sign
1	87	89	+
2	91	97	+
3	81	85	+
4	73	81	+
5	92	98	+
6	89	81	-

Brand B was liked better by 5 of 6 customers. Sample size was n = 6. The Binomial table (ST 1) yields the following: $p(x \geq 5) = .094 + .016 = .11$ and $(.11)(2) = .22 > .10$. The null hypothesis is accepted at the .10 level of significance. Customers rate the brands equally.